

Math 451 - Spring 2018

Homework 4

Due March 1st, 2018

You know, a tree is a tree, how many more do you need to look at?

— Ronald Reagan

Turn in:

- (1) Find all regular trees. Explain your answer.
- (2) Let G be a connected graph. We say a vertex x is a **cut-vertex** in G provided that $G - x$ is disconnected. What are all the cut-vertices of a nontrivial tree? Prove your answer.
- (3) Let G be a connected graph. Assume G contains two vertices u, v such that $G - u$ and $G - v$ are trees.
 - (a) Prove that $\deg u = \deg v$.
 - (b) Classify all connected graphs G with order $n \geq 3$ with the property that deleting any of its vertices gives a tree. (Hint: In this case G must be regular. What is this common degree?)
- (4) Find all trees T such that \overline{T} is also a tree.
- (5) Exercise 4.27
- (6) Exercise 4.39