

**Math 314 - Spring 2024**

**Practice problems 4 (Euler's Theorem, Fermat Primality Test, Dixon's Factorization)**

Quiz: April 24 2024

*Cryptography succeeds when it's no longer the weakest link.*

— Ron Rivest

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**Practice:**

- (1) Compute  $\varphi(55)$  and  $\varphi(54)$ .
- (2) Find  $10^{122} \pmod{55}$  without using a calculator.
- (3) Find the decryption function  $D(y)$  corresponding to the encryption function

$$E(x) \equiv x^7 \pmod{54}.$$

- (4) Compute  $3^{14} \pmod{15}$ . What does this tell you about the primality/compositeness of 15?
- (5) Use the fact that  $17^2 = 289 \equiv 16 = 4^2 \pmod{91}$  to factor 91 using the factoring trick.