

MATH 314 Fall 2023 - Class Notes

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Summary: Other Forms Of Multi-Block SAES Encryption.

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Notes: Symbols used

- C_i = blocks of encrypted/Cipher text
- X_i = blocks of plain text
- IV = Initial Value
- $E_k(X_i)$ = the encryption of X_i
- $D_k(C_i)$ = the decryption of Cipher text

I. Modes of Operation

1. Electronic Code Book (ECB)

A. Encryption

Formula: $C_1 = E_k(X_1)$

B. Decryption

Formula: $X_1 = D_k(C_1)$

2. Cipher Block Chaining (CBC)

A. Encryption

Formulas:

$$IV = C_0$$

$$C_i = E_k(X_i \oplus C_{i-1}) \rightarrow C_1 = E_k(X_1 \oplus C_0) \rightarrow C_2 = E_k(X_2 \oplus C_1) \dots$$

B. Decryption

Formula:

$$D_k(C_1) = X_1 \oplus C_0 \rightarrow X_1 = D_k(C_1) \oplus C_0 \rightarrow X_i = D_k(C_i) \oplus C_{i-1}$$

3. Cipher Feed Back (CFB)

A. Encryption

Formulas:

$$IV = C_0$$

$$C_i = E_k(C_{i-1}) \oplus X_i \rightarrow C_1 = E_k(C_0) \oplus X_1$$

B. Decryption

Formula:

$$X_i = E_k(C_{i-1}) \oplus C_i$$

4. Output Feed Back(OFB)

A. Encryption

Formulas:

$$IV = O_0$$

$$O_i = E_k(O_{i-1})$$

$$C_i = X_i \oplus O_i$$

B. Decryption

Formula:

$$X_i = C_{i-1} \oplus O_i$$

5. Counter (CTR)

A. Encryption

Formulas:

$$IV = CTR_0$$

$$CTR_i = CTR_{i-1} + 1 \pmod{2}$$

1 increases by 1 for every subsequent blocks encrypted IE block 26 would make 1 increase to 26

$$CTR_i = CTR_{i-1} + i$$

+i is added as a binary number with normal binary addition rules 5 becomes 0101 so on

$$C_i = E_k(CTR_i) \oplus X_i$$

B. Decryption

Formula:

$$X_i = E_k(CTR_i) \oplus C_i$$