Math 314 - Fall 2017 Mission 2

Name:

Due September 14, 2017

There are two kinds of cryptography in this world: cryptography that will stop your kid sister from reading your files, and cryptography that will stop major governments from reading your files. — Bruce Schneier

- All work must be shown for full credit.
- You may use Sage to help you solve the problems. If you do, print out your code.
- Either print out this assignment and write your answers on it, or edit the latex source and type your answers in the document. You must still show your work!
- You may work with classmates, but be sure to turn in your own written solutions. Write down the name(s) of anyone who helps you.
- <u>Check one:</u>
 - \Box I worked with the following classmate(s): _____

I did not receive any help on this assignment.

1. Graded Problems

1. Eve is listening in on messages being sent by Alice to Bob using a Vigenere cipher. At some point Eve captures the message:

DMNVTCDMNVTQ

She suspects that something fell on Alice's keyboard, causing her to send the same letter repeatedly. Explain why Eve might think this, and figure out the keyword Alice and Bob were using.

2. Determine which of the matrices $A = \begin{pmatrix} 2 & 9 \\ 3 & 7 \end{pmatrix}$, $B = \begin{pmatrix} 5 & 7 \\ 2 & 3 \end{pmatrix} C = \begin{pmatrix} 2 & 4 \\ 3 & 6 \end{pmatrix}$ and $D = \begin{pmatrix} 5 & 11 \\ 1 & 4 \end{pmatrix}$ are valid matrices for the Hill Cipher and find the decryption matrices for those that are. (Remember, you can't have any fractions modulo 26! All of your matrices should only contain numbers between 0 and 25.)

3. The ciphertext ELNI was encrypted by a Hill cipher with a 2×2 matrix. The plaintext is dont. Find the encryption matrix M.

4. a. Let a, b, c, d, e, f be integers (mod 26). Consider the following combination of the Hill and affine ciphers: represent a block of plaintext as a pair $(x, y) \pmod{26}$. The corresponding ciphertext (u, v) is

$$(x,y) \begin{pmatrix} a & b \\ c & d \end{pmatrix} + (e,f) \equiv (u,v) \pmod{26}.$$

Encrypt the plaintext here using the values below:

$$(x,y) \left(\begin{array}{cc} 3 & 4\\ 3 & 1 \end{array}\right) + (8,11) \equiv (u,v) \pmod{26}$$

b. Describe how to perform a chosen plaintext attack on this system (with the goal of finding the key a, b, c, d, e, f) State the plaintexts you chose and how to recover the key.

2. Recommended Exercises

These will not be graded but are recommended if you need more practice.

• Section 2.13: # 10, 13