MATH 314 - Class Notes

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 $\underbrace{\mathbf{Summary:}}_{\text{System.}}$ Todays class covered the introduction to DES and the general format for a Feistel

Notes:

<u>DES</u>- Data Encryption Standard

It was a form of Encryption used for almost all digital communication from the 70's till around 2000.

It is still used today in legacy applications, mainly banking.

History: In 1972 NBS (now NIST) put out a request for a new Cryptosystem. IBM Submitted their system (LUCIFER). NSA made changes to LUCIFER and the result was published in 1975 as DES. In 1990 Biham and Shamir published a technique called differential cryptanalysis that could crack a DES like system using 15 rounds (DES uses 16).

Overall Philosophy: Diffusion and Confusion

- <u>Diffusion</u>: Small changes in the plaintext have big changes on the ciphertext. Ideally changing one bit of the plaintext should change about half the digits of the ciphertext.
- <u>Confusion</u>: Every bit of the ciphertext should depend on the entire key in a way that is hard to predict.

Simplified DES (SDES):

DES is a Feistel System:

- We work with $bits(F_2)$
- Use \oplus to denote bitwise addition in F_2
- Write our plaintext in binary and split it into two halves $> L_0$ and R_0 (have m bits each)
- Choose *n* different keys $(k_0, k_1, ..., k_n)$ *n*=number of rounds

Define a function (R_i, k_{i+1}) that outputs m bits. Encryption: Get the i^{th} step from the $i - 1^{th}$ step.

 $L_i = R_{i-1}$ $R_i = L_{i-1} \oplus f(R_{i-1}, k_i)$

 R_{i-1} becomes L_i $L_{i-1} \oplus f(R_{i-1}, k_i)$ becomes R_i Repeat this process n times.

Decryption: Key fact is that in $F_2(x \oplus y) \oplus y = x$ Swap L_n and R_n Repeat encryption steps with keys: $k_n, k_{n-1}, ..., k_1$ Repeat n times

 $L_n = R_{n-1}$ $R_n = L_{n-1} \oplus f(R_{n-1}, k_n)$

SDES

- Messages will have 12 bits
- L_0, R_0 will have 6 bits
- Master key: 9 bit string
- Keys k_i is the 8 bits of the master key starting with bit i and wrapping around.

Examples: k = 101100110 $k_1 = 10110011$ $k_2 = 01100110$ $k_3 = 11001101$ $k_4 = 10011010$

Define $f(R_{i-1}, k_1)$:

First: Need an expander function (Diffusion Step) E(x) function that takes in 6 bits and outputs 8.

123456 turns into: 12434356

Ex: E(101011) : 10010111

Second: S-Box (Confusion Step) S-Box takes in 4 bits and outputs 3 bits

 $S_1 =$ (0) 101 010 001 110 011 100 111 000 (1) 001 100 110 010 000 111 101 011

$$\begin{split} S_2 = \\ (0) \ 100 \ 000 \ 110 \ 101 \ 111 \ 001 \ 011 \ 010 \\ (1) \ 101 \ 011 \ 000 \ 111 \ 110 \ 010 \ 001 \ 100 \end{split}$$

The first bit determines the row to use in the S-box The last 3 bits (that number) describes which column to use Example:

 $S_1(1110)$ The first deterimes that it is the second row. The 110 is in Decimal 6 meaning the 6th (or 7th when starting with the first row being 1) meaning the output is 101.

 R_{i-1} which is 6 bits is fed into the expansion function, making it 8 bits. It is then \oplus with k_i which would still be 8 bits. Then that is split in half, with the upper left most half being fed into S_1 and lower fed into S_2 . After that they are both put together as the output.

Try yourself with Message [100001111000] and Master Key: 110010110 using the formula: $L_i = R_{i-1}$ $R_i = L_{i-1} \oplus f(R_{i-1}, k_i)$ k = 110010110 $k_1 = 11001011$ $k_2 = 10010110$ $k_3 = 00101101$ $L_0 = 100001 \ R_0 = 111000$ $L_1 = 111000 \ R_1 = L_0 \oplus f(R_0, k_1)$ E(111000) = 11010100 $11010100 \oplus 11001011 = 00011111$ $S_1(0001) = 010$ $S_2(1111) = 100$ Output = 010100Finally $R_1 = 100001 \oplus 010100 = 110101$ Repeat until n = 4