

Math 275 - Spring 2016
Practice Midterm Questions

- (1) Identify the surface whose equation is given in cylindrical coordinates.
- (a) $z = 4 - r^2$.
 - (b) $2r^2 + z^2 = 1$.
- (2) Identify the surface whose equation is given in spherical coordinates.
- (a) $\rho = \sin \theta \sin \phi$.
 - (b) $\rho^2(\sin^2 \phi \sin^2 \theta + \cos^2 \phi) = 9$.
- (3) Find the angle between the given vectors, find the projection of \mathbf{a} in the direction of \mathbf{b} , and find a unit vector orthogonal to both of them.
- (a) $\mathbf{a} = \langle 1, -1, 3 \rangle$, $\mathbf{b} = \langle 1, 2, -1 \rangle$
 - (b) $\mathbf{a} = \langle 3, -3, 2 \rangle$, $\mathbf{b} = \langle 1, -1, 5 \rangle$
- (4) Find the area of the triangle with vertices $A(1, 1, 1)$, $B(1, -1, 2)$, $C(0, 2, 3)$.
- (5) Determine whether the lines L_1 and L_2 are parallel, skew or intersecting. If they intersect find the point of intersection.
- (a) $L_1: \frac{x-2}{1} = \frac{y-3}{-2} = \frac{z-1}{-3}$. $L_2: \frac{x-3}{1} = \frac{y+4}{3} = \frac{z-2}{-7}$.
 - (b) $L_1: x = 3 + 2t, y = 4 - t, z = 1 + 3t$. $L_2: x = 1 + 4s, y = 3 - 2s, z = 4 + 5s$.
- (6) Find vector and linear equations for each plane.
- (a) The plane containing the point $(1, 3, 2)$ with normal vector $\langle 2, -1, 5 \rangle = 0$.
 - (b) The plane containing the points $(2, 0, 3)$, $(1, 1, 0)$ and $(3, 2, 1)$.
 - (c) The plane containing the point $(1, 2, 1)$ and perpendicular to the planes $x + y = 2$ and $2x + y - z = 1$.
- (7) Find the distance between the point $(2, 0, 1)$ and the plane $2x - y + 2z = 4$. $\frac{2}{3}$
- (8) Find the equation of the tangent line to the curve $\mathbf{r}(t) = \langle t, 4 \sin(\pi t), t^2 - 1 \rangle$ at the point $(2, 4, 3)$.
- (9) Find the arclength of $\mathbf{r}(t) = \langle e^t, e^{-t}, t\sqrt{2} \rangle$ for $0 \leq t \leq 2$.
- (10) **(Corrected)** Find the point of intersection and the angle between the curves $\mathbf{f}(s) = \langle s, s^2, s^2 + s \rangle$ and $\mathbf{g}(t) = \langle t - 3, 1, t^2 - 4 \rangle$.
- (11) For each function draw the level curves and describe the graph of the function.
- (a) $f(x, y) = 2x^2 - y$.
 - (b) $f(x, y) = (x - 2)^2 + (y + 1)^2$.
- (12) Find the limit if it exists, or show that the limit does not exist.
- (a) $\lim_{(x,y) \rightarrow (0,0)} \frac{x^4 - 4y^2}{x^2 + 2y^2}$.
 - (b) $\lim_{(x,y) \rightarrow (0,0)} \frac{3x^3 \cos(y)}{2x^3 + y^5}$.
 - (c) $\lim_{(x,y) \rightarrow (1,2)} \frac{((x-1)^2 + (y-2)^2)^2}{(x-1)^2 + (y-2)^2}$

(13) Classify each surface.

(a) $x^2 - y^2 + z^2 - 4x - 2z = 0$.

(b) $4x^2 + y^2 + z^2 - 24x - 8y + 4z + 55 = 0$.