## Math 275 - Spring 2016 **Practice Midterm Questions**

- (1) Identify the surface whose equation is given in cylindrical coordinates.
  - (a)  $z = 4 r^2$ .
  - (b)  $2r^2 + z^2 = 1$ .
- (2) Identify the surface whose equation is given in spherical coordinates.
  - (a)  $\rho = \sin \theta \sin \phi$ .
  - (b)  $\rho^2(\sin^2\phi\sin^2\theta + \cos^2\phi) = 9$ .
- (3) Find the angle between the given vectors, find the projection of **a** in the direction of **b**, and find a unit vector orthogonal to both of them.
  - (a)  $\mathbf{a} = \langle 1, -1, 3 \rangle, \ \mathbf{b} = \langle 1, 2, -1 \rangle$
  - (b)  $\mathbf{a} = \langle 3, -3, 2 \rangle, \ \mathbf{b} = \langle 1, -1, 5 \rangle$
- (4) Find the area of the triangle with vertices A(1,1,1), B(1,-1,2), C(0,2,3).
- (5) Determine whether the lines  $L_1$  and  $L_2$  are parallel, skew or intersecting. If they intersect find the point of intersection.
  - (a)  $L_1$ :  $\frac{x-2}{1} = \frac{y-3}{-2} = \frac{z-1}{-3}$ .  $L_2$ :  $\frac{x-3}{1} = \frac{y+4}{3} = \frac{z-2}{-7}$ .
  - (b)  $L_1$ : x = 3 + 2t, y = 4 t, z = 1 + 3t.  $L_2$ : x = 1 + 4s, y = 3 2s, z = 4 + 5s.
- (6) Find vector and linear equations for each plane.
  - (a) The plane containing the point (1,3,2) with normal vector (2,-1,5)=0.
  - (b) The plane containing the points (2,0,3), (1,1,0) and (3,2,1).
  - (c) The plane containing the point (1,2,1) and perpendicular to the planes x+y=2and 2x + y - z = 1.
- (7) Find the distance between the point (2,0,1) and the plane 2x-y+2z=4.
- (8) Find the equation of the tangent line to the curve  $\mathbf{r}(t) = \langle t, 4\sin(\pi t), t^2 1 \rangle$  at the point (2,4,3).
- (9) Find the arclength of  $\mathbf{r}(t) = \langle e^t, e^{-t}, t\sqrt{2} \rangle$  for  $0 \le t \le 2$ .
- (10) (Corrected) Find the point of intersection and the angle between the curves  $\mathbf{f}(s) =$  $\langle s, s^2, s^2 + s \rangle$  and  $\mathbf{g}(t) = \langle t - 3, 1, t^2 - 4 \rangle$ .
- (11) For each function draw the level curves and describe the graph of the function.
  - (a)  $f(x,y) = 2x^2 y$ .
  - (b)  $f(x,y) = (x-2)^2 + (y+1)^2$ .
- (12) Find the limit if it exists, or show that the limit does not exist.
  - (a)  $\lim_{(x,y)\to(0,0)} \frac{x^4 4y^2}{x^2 + 2y^2}$ .

  - (b)  $\lim_{(x,y)\to(0,0)} \frac{3x^3 \cos(y)}{2x^3 + y^5}.$ (c)  $\lim_{(x,y)\to(1,2)} \frac{((x-1)^2 + (y-2)^2)^2}{(x-1)^2 + (y-2)^2}$

- (13) Classify each surface. (a)  $x^2-y^2+z^2-4x-2z=0$ . (b)  $4x^2+y^2+z^2-24x-8y+4z+55=0$ .